### Principles of Radar an introductory view

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# Basic concepts

- EM signal transmission
- Signal reception
- Infer information about the 'target' by comparing received signal with transmitted signal

# EM signals

- Frequency, wavelength, polarization, and speed of light
- signals propagate at speed of light,  $c = 3 \times 10^8 \text{ m/s} = 1 \text{ foot/ns} [1 \text{ ns} = 10^{-9} \text{ s}]$ 
  - speed of light is ~ 1,000,000 time faster than
    speed of sound in air

# Reflection, refraction, attenuation, and scattering



# Reflection, refraction, attenuation, and scattering

- Reflection and refraction depend on material's electrical and magnetic properties, geometry, surface characteristics
- Attenuation (signal strength reduction) caused by absorption (energy converted to heat) and scattering
- Scattering depends on material's electrical and magnetic properties and size of scatterer (relative to wavelength) (why the sky is blue)

# Radar components

Timing and control Waveform generator Transmitter electronics Transmit antenna Receive antenna Receive electronics Data acquisition system Digital signal processor Ancillary sensors (e.g., GPS) Data storage device



# Radar Range Equation

Received signal power  $(P_r)$  depends on:

P<sub>t</sub>: transmitted signal power

G: antenna's ability to focus power on target

R: range to the target

 $\sigma$ : target's radar cross section

A<sub>e</sub>: antenna's ability to capture echo signal

$$P_{\rm r} = P_{\rm t} \frac{G}{4\pi R^2} \sigma \frac{1}{4\pi R^2} A_{\rm e}$$

which simplifies to

$$P_{\rm r} = \frac{P_{\rm t} \, \mathrm{G} \, \mathrm{\sigma} \, \mathrm{A}_{\rm e}}{\left(4\pi\right)^2 \mathrm{R}^4}$$

# What can be measured Target range

Transmitted signal is time-gated sinusoid,

$$\begin{split} s(t) &= A \, cos(2 \, \pi \, f_{TX} t + \phi_{TX}) \quad {\rm for} \, 0 \leq t \leq \tau \\ (\text{pulse duration is } \tau) \end{split}$$
 Received signal is

 $p(t) = B\cos\left[2\pi f_{TX} t + \phi_{TX} + \phi_{RX}\right] \text{ for } T \le t \le T + \tau$ 

Round-trip travel time,  $T = \frac{2R}{c}$  so  $R = \frac{cT}{2}$ 

and we can measure time with great precision

### Target Range - Altimeter



# Altimeter data



### Altimeter data



Global topographic map of ocean surface produced with satellite altimeter.

# What can be measured

### **Spatial extent of target**

### Antenna directs radar signal in narrow beam, rotating antenna enables radar to scene in a circular fashion





Radar antenna.

Radiation pattern of radar antenna.



# **Spatial extent of target**

17:32 08-JUN-2004 GMT @Copyright WSI Corporation http://www.wsi.com



Rain off the coast of Brownsville, Texas.

# **Spatial extent of target**



A flock of birds traveling north into south Texas from the Gulf of Mexico.

# *What can be measured* Relative radial velocity of target

Received signal phase,  $\phi_{RX}$ , is range dependent,  $\phi_{RX} = 2\pi \frac{2R}{\lambda}$ 

where  $\lambda$  is the signal wavelength,  $\lambda = c/f_{TX}$ 

If the range to the target changes, the received signal phase will change with time producing a Doppler shift,  $f_D$ , where

$$f_{\rm D} = \frac{\Delta \phi_{\rm RX}}{\Delta t}$$

which can be shown to be

$$f_{\rm D} = \frac{2v}{\lambda} \cos \theta$$

where  $\theta$  is the angle between the velocity vector and the radar's range vector. The received signal is  $p(t) = B \cos \left[2\pi (f_{TX} + f_D)t + \phi_{TX}\right]$  for  $T \le t \le T + \tau$ 

### **Relative radial velocity of target**

#### 17:38 08-JUN-2004 GMT @Copyright WSI Corporation http://www.wsi.com



Radial velocity of precipitation near Brownsville, Texas.

#### **Relative radial velocity of target**



Isorange and isodoppler lines for aircraft flying north at 10 m/s at a 1500-m altitude.  $\Delta R = 2 \text{ m}, \ \Delta V = 0.002 \text{ m/s}, \Delta f_D = 0.13 \text{ Hz} @ f = 10 \text{ GHz}, \lambda = 3 \text{ cm}$ 

# What can be measured

### **Target reflectivity**

Backscatter depends on material properties, local geometry (e.g., slope), surface roughness. By combining the ability to discriminate based on range and velocity (Doppler), images of radar backscatter can be formed.



### Real-aperture, side-looking airborne radar (SLAR) image of Puerto Rico





Mosaicked image composed of 48-km (30-mile) wide strip map images **Radar parameters** modified Motorola APS-94D system X-band (3-cm wavelength)

X-band (3-cm wavelength) altitude: 8,230 m (above mean sea level) azimuth resolution: 10 to 15 m

#### **Digital Elevation Model of Puerto Rico**



### **Target reflectivity**



Synthetic-aperture radar (SAR) geometry



SAR image of Los Angeles, CA area.

# SAR image of Gibraltar





**ERS-1 Synthetic Aperture Radar** 

f: 5.3 GHz ant: 10 m x 1 m ∆x = ∆y = 30 m orbit: 780 km

P<sub>TX</sub>: 4.8 kW B: 15.5 MHz f<sub>s</sub>: 19 MSa/s D<sub>R</sub>: 105 Mb/s



Nonlinear internal waves propagating eastwards and oil slicks can be seen.



# SAR imagery of Venus



#### Ka-band, 4" resolution Helicopter and plane static display

f: 35 GHz





#### Frequency Comparison – Ku vs. UHF



### Layover and foreshortening distortion



#### **SEASAT Synthetic Aperture Radar**

Launched: June 28, 1978Died: October 10, 1978orbit: 800 kmf: 1.3 GHz $P_{TX}$ : 1 kW $\tau$ : 33.8 µsB: 19 MHz $\theta$ : 23 ± 3°PRF: 1464 to 1647 Hzant: 10.7 m x 2.2 m $\Delta x = 18$  to 23 m $\Delta y = 23$  m



Figure 5-4. Example of radar image layover. Seasat image of the Alaska Range showing the top of a mountain imaged onto the glacier at its foot (center). Shadows are also present on many of the backslopes of these steep mountains. Illumination is from the top [from Ford et al., 1989].



### **SEASAT image of Ames, Iowa**



Figure 5-6. Ames, Iowa, with bright streaks due to rain-soaked ground

#### Fine resolution range imaging of a ground moving target MTI Image of a 2.5 Ton Truck



20

40

80

Doppler Bin

60

100



# Examples of SAR Imagery

Washington, D.C. mall area



Aerial photo, 8-m resolution (USGS)



SAR image, 1-m resolution (Sandia National Laboratory)

# Examples of SAR Imagery

Capitol building, Washington, D.C.



Aerial photo, 1-m resolution (USGS)



SAR image, 1-m resolution (Sandia National Laboratory)

### Multipass interferometry



Multipass interferometry. Same or similar SAR systems image common region at different times. Differences can be attributed to elevation (relief) or horizontal displacements. Third observation needed to isolate elevation effects from displacement effects.



Image covers 18.1 km in azimuth, 26.8 km in range. The azimuth direction is horizontal.



# Subsidence measurement

about 6 cm/yr

400000

390000

Easting (motors)



Damage associated with subsidence at 71st and Olive Avenues

### Earthquake displacements

On December 26, 2003 a magnitude 6.6 earthquake struck the Kerman province in Iran. 2.8 cm Ban 10 cm

radar intensity image

differential interferogram

Multipass ENVISAT SAR data sets from June 11, 2003, December 3, 2003 and January 7, 2004. The maximum relative movement change in LOS is about 48 cm and located near the city Bam. **ENVISAT SAR** launched March 1, 2002 f: 5.331 GHz orbit: 800 km antenna: 10 m x 1.3 m  $\Delta x = \Delta y = 28$  m 320 T/R modules @ 38.7 dBm each: 2300 W

### InSAR Coherent Change Detection



Reference SAR Image: Grassy Field



Current SAR Image: Grassy Field



CCD Image - Changes denoted by dark areas



### InSAR Coherent Change Detection



### Single-pass interferometry



Single-pass interferometry. Two antennas offset by known baseline.

### Topographic map of North America

Shuttle Radar Topography Mission (SRTM) STS-99 Shuttle Endeavour Feb 11 to Feb 22, 2000 Mast length 60 m C and X band SAR systems 30-m resolution

#### Bistatic Images of Antenna Range 1 Meter Resolution / July 28, 1994

#### **Bi-static SAR**

- Bi-static SAR places Transmitter and Receiver on separate vehicles
- Allows unusual geometries
  - stationary transmitter or receiver,
  - looking straight ahead





#### Radar Responsive Tag System



# Challenges in radar

#### <u>Weak received signal power</u> (spherical spreading loss) $P_R \propto P_T / (4\pi)^2 R^4$

	Basketball court	Sear's tower	Jet aircraft	Space station	Moon
R	(94') 29 m	(1450') 442 m	(30,000') 10 km	360 km	384,400 km
$1 / (4 \pi)^2 R^4$	$9 \times 10^{-9}$	$1.7 \times 10^{-13}$	$6.3 \times 10^{-19}$	$3.8 \times 10^{-25}$	$2.9 \times 10^{-37}$
P <sub>R</sub> *	0.0009 W	$1.7 \times 10^{-8} \text{ W}$	$6.3 \times 10^{-14} \text{ W}$	$3.8 \times 10^{-20} \text{ W}$	$2.9 \times 10^{-32} \mathrm{W}$

\* assumes  $P_T = 100 \text{ kW} = 10^5 \text{ W}$  (KANU effective broadcast power)

<u>Noise</u> (anything above absolute zero radiates thermal noise)  $P_N = kTB$ 

k = Boltzmann's constant ( $1.38 \times 10^{-23} \text{ J/K}$ )

T = temperature in Kelvin (normal room temperature is ~290 K)

B = bandwidth (Hz)

Bandwidth impacts the ability to measure range accurately or to resolve multiple targets at similar ranges, otherwise we'd set B to a very small value.

Range resolution,  $\rho$ , is bandwidth dependent,  $\rho = \frac{c\tau}{2} = \frac{c}{2B}$ 

# Challenges in radar

**Clutter** (one man's trash is another man's treasure) Example, when looking for subsurface targets (land mines, subglacial features, subterranean structures, etc.) the surface echo can obscure the desired echo.

Antennas (size ∝ wavelength) Key properties include: frequencies of operation (bandwidth), beamwidth, polarization, steerability, size, weight, cost.

# Different radar applications

- Weather radar (ascertains precipitation's location, intensity, and nature (snow vs. rain))
- Police radar
- Collision avoidance radar
- Ground-penetrating radar (archeology, geology, crime scene investigation, civil engineering, ...)
- Aircraft detection and tracking (military) (measures aircraft's altitude, speed, heading, type, ...)
- Projectile tracking (defense ICBM early warning radar, asteroid tracking, source of mortar fire)
- Imaging radar (geography, military, scientific exploration, surface elevation, etc.)

# Radar research thrusts

- Making smaller, more versatile radars (programmable, low cost, network of radars)
- Designing optimum radar for particular application (looking for water/ice on Mars, characterizing Europa's icy shell)
- Advanced signal processing (clutter rejection, super resolution, autofocus, ...)
- Bistatic or multistatic radar (new capabilities because of new geometry, detecting stealthy targets)
- Passive radar (take advantage of transmitters of opportunity: TV, FM, GPS, DirecTV, etc.)